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1. Mathematical Programming

2. Index Method. An approximation technique.

(1) Index Number : Man Hours Required in any plant
divided by Least man hours of any plant.

Operations Research Methods & Problem
Sasienni Wiley

Linear Programming

Factors in Identity and constants must be positive

a. Restrictions $\leq \begin{cases} 7x + 6y \leq 84 \\ 7x + 6y + w_1 = 84 \end{cases}$

b. Requirements $\geq \begin{cases} 5x + 2y \geq 15 \\ 5x + 2y - w_2 + w_3 = 15 \end{cases}$

c. Approximation $\approx \begin{cases} 6x + 5y \approx 50 \\ 6x + 5y - w_3 + w_4 = 50 \end{cases}$

x	y	w ₂	w ₃	w ₁	w ₄
7	6			1	
5	2	-1			1
6	5	-1			1

z b o -1 o -1 -1

d. Equations $\begin{cases} 3x + 4y = 100 \\ 3x + 4y + w_2 = 100 \end{cases}$

\uparrow
 $-M$

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Object Column	Variable Column	Constant Column	Key Column	Penalty Column	Check Column				
			2 X	3 Y	0 W ₁	0 W ₂			
0 W ₁	30	3	4	1		38			objective row
0 W ₂	60	2	5	.	1	68			variable row
	0	-2	-3	0	0	-5			
3 Y	$\frac{30}{4}$	$\frac{3}{4}$	1	$\frac{1}{4}$	0	$\frac{3}{4}$			Index row
W ₁	$\frac{90}{4}$	$-\frac{7}{4}$	0	$-\frac{5}{4}$	1	$\frac{82}{4}$			Main Row
	$\frac{90}{4}$	$\frac{1}{4}$	0	$\frac{3}{4}$	0	$\frac{94}{4}$			Index row

repeat iteration until no negative numbers in each row.

Index Number = $\sum \{ \text{(number in col)} \text{ (corresponding number in obj col)} \} - \text{(No in object row at head of col)}$

$$(3.0) + (2.0) - 2 = -2$$

Key row = Dividing Constant column by Key col.

$$W_1 = \frac{30}{4} = 7.5; W_2 = \frac{60}{5} = 12 \text{ choose smallest}$$

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positive ratio.

Key Number: common element in key row and key column

Main Row: divide each number in key row by key number -

Element in new tableau = Corresponding element in old tableau - $\left(\frac{\text{corresponding element in key row} \times \text{corresponding element in key column}}{\text{key number}} \right)$

$$= 60 - \left(\frac{30 \times 5}{4} \right) = \frac{90}{4} = \frac{45}{2}$$

$$= 2 - \frac{3 \times 5}{4} = -\frac{7}{4}$$

$$= 5 - \frac{4 \times 5}{4} = 0$$

$$= 0 - \frac{1 \times 5}{4} = -\frac{5}{4}$$

$$= 1 - \frac{0 \times 5}{4} = 1$$

$$= 68 - \frac{38 \times 5}{4} = 68 - \frac{190}{4} = \frac{82}{4}$$

$$= 0 - \frac{30(-3)}{4} = \frac{90}{4}$$

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Variations on Simplex Problem

Idle time process I cost $\$ \frac{1}{2}$

Idle time process II Cost $\$ 1$

Object row modify 2 1 0 3 $-\frac{1}{2}$ $-\frac{1}{2}$

~~allowable only and in~~

~~piece y and 0~~

$$2x + 3y - \frac{1}{2}w_1 - w_2 = \text{min.}$$

— + —

Maximum no of pieces $x + y = \text{Max}$

objective now 1 1 0 0

— + —

Another requirement $x = 4$

$$x + w_3 = 4$$

attach high cost to w_3 arbitrarily which would make it disappear.

Minimize idle time $w_1 + w_2$ becomes
 $-w_1 - w_2$